

# Center for Environmental & Applied Fluid Mechanics

## “Vortical and Wave Modes in Rotating Stratified Turbulence”

**Presented by**  
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Utilizing an eigenfunction decomposition, we study the growth and spectra of energy in the vortical (geostrophic) and wave (ageostrophic) modes of a three-dimensional (3D) rotating stratified fluid as a function of  $\beta = f/N$ , where  $f$  is the Coriolis parameter and  $N$  is the Brunt-Vaisala frequency. Working in regimes characterized by moderate Burger numbers, i.e.  $Bu = 1/\beta < 1$  or  $Bu \geq 1$ , our results indicate profound change in the character of vortical and wave mode interactions with respect to  $Bu = 1$ . As with the reference state of  $\beta = 1$ , for  $\beta < 1$  the wave mode energy saturates quite quickly and the ensuing forward cascade continues to act as an efficient means of dissipating ageostrophic energy. Further, these saturated spectra steepen as  $\beta$  decreases: we see a shift from  $k^{-1}$  to  $k^{-5/3}$  scaling for  $k_f < k < k_d$  (where  $k_f$  and  $k_d$  are the forcing and dissipation scales, respectively). On the other hand, when  $\beta > 1$  the wave mode energy never saturates and comes to dominate the total energy in the system. In fact, in a sense the wave modes behave in an asymmetric manner about  $\beta = 1$ . With regard to the vortical modes, for  $\beta \approx 1$ , the signatures of 3D quasigeostrophy are clearly evident. Specifically, we see a  $k^{-3}$  scaling for  $k_f < k < k_d$  and, in accord with an inverse transfer of energy, the vortical mode energy never saturates but rather increases for all  $k < k_f$ . In contrast, for  $\beta > 1$  and increasing, the vortical modes contain a progressively smaller fraction of the total energy indicating that the 3D quasigeostrophic subsystem, though always present, plays an energetically smaller role in the overall dynamics.

**Friday, November 7, 2008**  
**11:00 a.m., 110 Maryland Hall**